

Figure 3 Radar cross section versus scattering angle for Case 2 after 100 realizations

TABLE 1 Comparison of CPU Seconds on a vax-6000-350

Matrix Inversion	BMIA One iteration	BMIA Five iterations	KI Five iterations
Case 1	23.16	0.98	2.07
Case 2	22.94	0.92	2.05

cident angle is  $20^\circ$  from normal. Figure 1 shows the comparison of total field on the rough surface for Case 1 for a single realization; both BMIA and KI agree well with EMI after five iterations. It should be noted that BMIA is more accurate than KI at the two edges of the surface. Figures 2 and 3 show the ensemble average of 100 realizations of radar cross section of the rough surface for Cases 1 and 2, respectively. For Case 1, BMIA agrees very well with EMI after five iterations. Both BMIA with one iteration and KI with five iterations give the general trend of the EMI. Backscattering enhancement is observed. Thus the first-order solution of BMIA already gives backscattering enhancement. For Case 2, however, both BMIA with both one and five iterations agrees very well with EMI when KI yields erroneous results. The CPU time for solving the matrix equation using EMI, BMIA, and KI is listed in Table 1. It is shown that BMIA is much faster than EMI and is comparable to KI. BMIA continues to work when KI fails.

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## MEASUREMENT OF THE TEMPORAL COHERENCE OF AN UNDERWATER OPTICAL SCATTERED FIELD

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#### KEY TERMS

Temporal coherence, scattering, heterodyning

#### ABSTRACT

The coherence of a laser signal propagating through a turbid medium deteriorates due to scattering, affecting the performance of un-



## I. INTRODUCTION

The coherence properties of narrow spectral linewidth laser signals have proved to be of great importance in imaging, communications, optical sensing, and measurements. However, for applications in a medium with suspended particles, such as ocean waters, the coherence characteristics change due to the scattering of light, impairing the performance of optical systems. Image processing techniques based on the difference between the temporal coherence of the unscattered laser signal and the strong background illumination including scattered signal can achieve a large degree of image enhancement [1].

The laser beam in line-of-sight propagation is always a mixture of the incident and scattered light. The total field is almost coherent for a short distance from the transmitter since scattering is significant. At a greater distance, however, the total field becomes less coherent due to scattering, although the field collected at a narrow receiving angle is predominantly coherent. At a large distance, when the main beam has been significantly attenuated due to scattering and absorption, the total field approaches total incoherence. Both singly and multiply scattered radiation is of importance for optical systems in which the transmitter and receiver are widely separated. The actual amount of received forward-scattered power depends on the properties of the medium, receiver area, angular field of view, and the beam characteristics.

To assist in characterizing the coherence properties of a laser beam, the instantaneous scattered field can be regarded as the superposition of waves scattered from the individual scattering centers. This scattered field therefore fluctuates in response to the motion of the scatterers. The detection method used in a particular experiment depends on the time

scale of these fluctuations. Filter methods are used to study relatively rapid molecular dynamic processes, that is, those that occur on a time scale faster than about  $10^{-6}$  sec. Optical mixing or heterodyning methods are usually used for processes that occur on time scales slower than about  $10^{-6}$  sec [2]. The scattered signal from particles of size comparable to or larger than the laser signal wavelength shows a Doppler effect due to the Brownian motion of the particles and turbulence in ocean waters. In the study reported in this article the coherence times of the unscattered laser signal along with the scattered field, and that of the scattered field only, have been evaluated from the autocorrelation function, obtained using a Mach-Zehnder interferometer followed by digital signal processing. The coherence time of the laser beam has also been measured in air using a Michelson interferometer [3].

## II. EXPERIMENTAL PROCEDURE

The modified Mach-Zehnder interferometric system is arranged as shown in Figure 1. The reference beam is shifted by  $\Omega$  and propagates through air. The second (affected beam) propagates through a 1.2-m water path with suspended particles. As the affected beam exits the tank, it contains two parts: (i) a central beam without any appreciable scattering and (ii) the scattered signal around this central beam. In the first experiment both the parts (that is, the central unscattered beam plus the scattered light up to angle  $\Psi = 2.4^\circ$  off the optical axis) are collected by a lens and heterodyned with the reference beam using a photomultiplier tube that provides current output signal proportional to the light intensity. In the second experiment, the central beam is blocked and only the scattered light is collected and heterodyned with the reference beam.

The heterodyned output current is connected to a digital oscilloscope that provides a convenient means for digitizing the current signal. The signal is digitized into 1028 sample points at 8-bit resolution and is stored in the oscilloscope

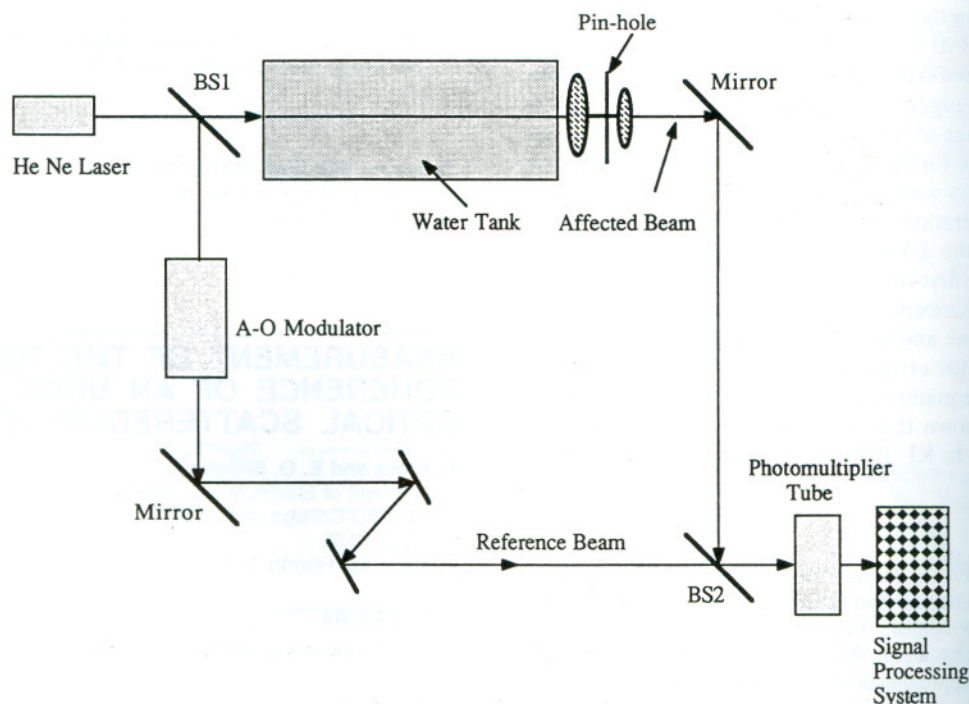


Figure 1 Mach-Zehnder interferometer



memory. The data from the digital oscilloscope are transferred to another computer for further signal processing.

### III. DETERMINATION OF COHERENCE TIME

Using the interferometric system the output current of the photomultiplier can be expressed as

$$i_d(t) = E_1^2 + E_2^2 + 2E_1E_2 \cos[(\Omega - \omega_D)t + \Theta_r(t) - \Theta_w(t)], \quad (1)$$

where  $E_1$  and  $E_2$  are the field amplitudes of the reference beam and the affected beam, respectively,  $\Theta_w$  and  $\Theta_r$  are the random phase shifts of the affected and reference beams, respectively, and  $\omega_D$  is the random frequency shift due to the Doppler effect introduced by the water path [4]. The estimated autocorrelation function is

$$R(\tau) = \langle i_d(t + \tau) i_d^*(t) \rangle, \quad (2)$$

where the angular brackets indicate time averaging. The estimated autocovariance from Eq. (2) is

$$C(\tau) = \langle i_d(t + \tau) i_d^*(t) \rangle - \bar{i}_d^2, \quad (3)$$

where  $\bar{i}_d^2$  is the average value of the square of the current  $i_d(t)$  over the time interval of interest.

The random Doppler shift due to turbulence and the Brownian motion of the suspended particles,  $\omega_d$ , is assumed to have a Gaussian probability density distribution with variance  $\sigma^2$ . The variance  $\sigma^2$  is a function of wavelength of radiation, path length, medium quality, temperature, and turbulence conditions, etc. Also in Eq. (1), assuming  $\Theta_r \approx \Theta_w \approx 0$ , it can be shown that the autocovariance function is Gaussian and is expressed as

$$C(\tau) = E_1^2 \cdot E_2^2 \cos(\Omega\tau) \exp(-\sigma^2\tau^2/2) \\ = C_e(\tau) \cos(\Omega\tau), \quad (4)$$

where  $C_e(\tau)$  is the envelope of  $C(\tau)$ .

The coherence time is defined as [2]

$$\tau_c = \int_0^\infty \frac{C_e(\tau)}{C_e(0)} d\tau. \quad (5)$$

Substituting Eq. (4) into Eq. (5) and simplifying.

$$\tau_c = 1.25 \sigma.$$

The value of the covariance function envelope  $C_e(\tau)$  at  $\tau_c$  is

$$C_e(\tau = 1.25\sigma) = 0.456C_e(0). \quad (6)$$

This shows that the coherence time  $\tau_c$  corresponds to the time at which the envelope of the covariance function is 0.456 of its peak value  $C(\tau = 0)$ . To compute  $C(\tau)$  from experimental values of  $i_d$  over a time  $T$ ,  $i_d$  is sampled and stored as  $N$  discrete values. Thus, the sampling interval is  $\Delta t = T/N$ , and the sample time can be expressed as  $t = n \Delta t$ , where  $n$  is an integer index ranging from 0 to  $N - 1$ . The discrete correlation parameter  $\tau$  can similarly be expressed as  $k \Delta t$ , where  $k$  is an integer index. With this notation and converting

the integral to a sum, the autocorrelation function in discrete form is

$$R(k \Delta t) = \frac{1}{N} \sum_{n=0}^{N-1} i_d(n \Delta t) \cdot i_d(n \Delta t + k \Delta t). \quad (7)$$

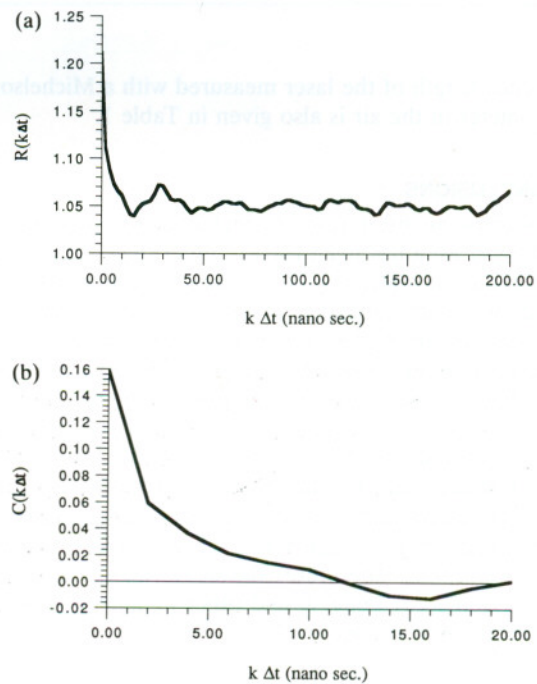
The corresponding autocovariance function in discrete form is

$$C(k \Delta t) = R(k \Delta t) - \frac{1}{N} \sum_{n=0}^{N-1} i_d^2(n \Delta t). \quad (8)$$

Using this equation the covariance function is computed and graphed. The coherence time  $\tau_c$  is computed based on Eq. (6) using an extrapolation technique.

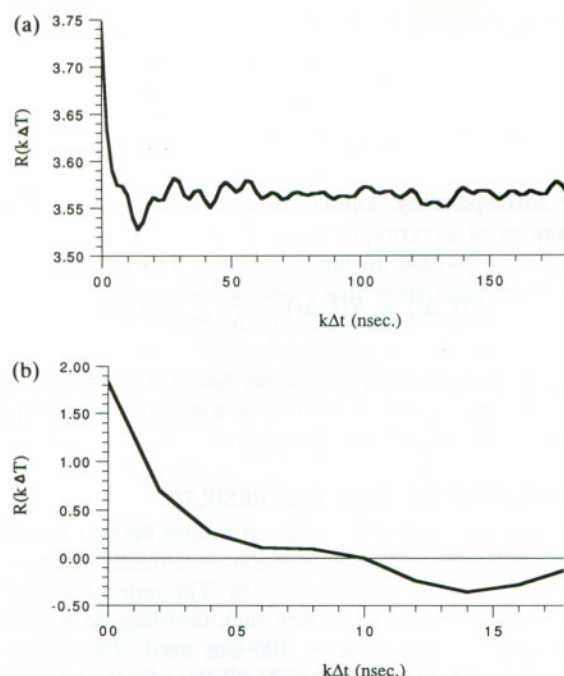
### IV. EXPERIMENTAL DATA AND RESULTS

Measurements of the heterodyned output current for determining the autocorrelation function were made with  $\Omega = 80$  MHz,  $T = 20$  nsec, and  $N = 1028$ . The index  $k$  in Eq. (8) is arbitrary but must be chosen such that  $k_{\max} \Delta t \ll N \Delta t$  or  $k_{\max} \ll N$ . A value of  $K = 100$  was used. The calculated autocorrelation functions for the scattered signal only, and the scattered field plus the central laser beam, are graphed in Figures 2(a) and 3(a), respectively. The corresponding autocovariance functions are graphed in Figures 2(b) and 3(b). The peak value of autocovariance function,  $C(0)$ , is the calculated value for  $k = 0$ . This value is multiplied by 0.456 to establish the value at which  $\tau_c$  is to be determined. Since the time corresponding to  $0.456C(0)$  may not align with a  $k \Delta t$ , it is necessary to perform an interpolation between the two nearest  $k \Delta t$  points. The computed values of coherence time  $\tau_c$  and length  $l_c$  are tabulated in Table 1. For comparison the



**Figure 2** (a) Autocorrelation function versus  $k \Delta t$  for scattered signal only. Signal duration  $T = 20 \mu\text{sec}$ ,  $\Delta t = 2$  nsec. (b) Autocovariance function versus  $k \Delta t$  for scattered signal only. Signal duration  $T = 20 \mu\text{sec}$ ,  $\Delta t = 2$  nsec





**Figure 3** (a) Autocorrelation function versus  $k \Delta t(\tau)$  for scattered signal plus direct laser beam. Signal duration  $T = 20 \mu\text{sec}$ ,  $\Delta t = 2 \text{ nsec}$ . (b) Autocovariance function versus  $k \Delta t(\tau)$  for scattered signal plus direct laser beam. Signal duration  $T = 20 \mu\text{sec}$ ,  $\Delta t = 2 \text{ nsec}$

**TABLE 1** Coherence Time and Coherence Length

Only Scattering $\tau_c$ (nsec)	$l_c$ (cm)	Direct Beams Scattering		Laser Signal (Michelson Interferometer)	
		$\tau_c$ (nsec)	$l_c$ (cm)	$\tau_c$ (nsec)	$l_c$ (cm)
1.6	48	1.9	57	$\approx 9.0$	$\approx 270.0$

coherence length of the laser measured with a Michelson interferometer in the air is also given in Table 1.

## V. CONCLUSIONS

In this article an interferometric technique followed by digital signal processing has been used to determine the loss in coherence due to scattering in simulated ocean waters. Comparing the results tabulated in Table 1, it is noted that the coherence length of the laser signal in air as measured using a Michelson interferometer is on the order of 270 cm. In a water medium, the coherence length of the scattered signal reduces to  $\approx 48 \text{ cm}$ , whereas the coherence length of scattered plus unscattered signal is between these two values. This is to be expected, since the direct unscattered beam contributes to the collected light and has greater coherence length. Clearly, scattering through water has a significant effect on coherence length. Therefore, the design of underwater coherent systems for imaging and other applications needs to consider the loss in coherence.

## ACKNOWLEDGMENTS

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## ERRATA "VERNIER FIBER DOUBLE-RING RESONATOR USING DEGENERATE TWO-WAVE MIXING"

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There are a few typographical errors in Reference [1]. The right-hand side of Eq. (1) should be multiplied by  $a_1^2$ , that of Eq. (2) by  $a_2^2$ , and that of Eq. (4) by  $a^4$ . In Eqs. (6) and (7),  $t_1$  should read  $t_2$ .

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## ERRATA "CALCULATION OF S PARAMETERS FROM ABCD PARAMETERS WITH COMPLEX NORMALIZING IMPEDANCES"

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The above article [1] appears with three typographical errors. On page 613, the equation for  $V_{ji}$  should read

$$V_{ji} = a_j \cdot Z_{0j}^* \cdot \left[ \frac{2}{Z_{0j} + Z_{0j}^*} \right]^{1/2}$$